

RESEARCH ARTICLE

Autonomous Utility Network Regulation through Data Driven Algorithms with Load Forecasting Techniques

Dr. Ahmed Said Mohamed

Department of Computational Intelligence and Energy Technologies, Comoros Research University, Comoros

VOLUME: Vol.05 Issue07 2026

PAGE: 01-07

Copyright © 2026 Journal of Multidisciplinary Sciences and Innovations, This is an open -access article distributed under the terms of the Creative Commons Attribution-Noncommercial-Share Alike 4.0 International License. Licensed under Creative Commons License a Creative Commons Attribution 4.0 International License.

Abstract

The rapid transformation of conventional utility networks into intelligent, decentralized, and adaptive infrastructures has created a need for advanced regulation mechanisms capable of managing uncertainty, increasing operational complexity, and integrating diverse energy resources. Autonomous utility network regulation through data-driven algorithms and load forecasting techniques represents a significant research direction for achieving reliable, efficient, and resilient power system operation. This research paper investigates the conceptual framework, technical architecture, and operational implications of applying artificial intelligence-based regulation, predictive analytics, and intelligent control methodologies in modern utility networks. The study synthesizes existing theoretical approaches related to microgrid control, distributed energy resource management, congestion regulation, and predictive energy management to develop an integrated perspective on autonomous utility regulation.

The analysis demonstrates that autonomous regulation can improve grid reliability, reduce operational losses, enhance renewable energy integration, and support efficient congestion management. Data-driven approaches provide opportunities for utilities to transition from static operational rules toward adaptive systems capable of responding to changing demand patterns and generation uncertainties. Recent developments in artificial intelligence and predictive analytics emphasize the importance of intelligent energy management frameworks for future smart grid environments (Philip, 2025). However, challenges related to data quality, computational complexity, cybersecurity, regulatory compliance, and model adaptability remain significant barriers to large-scale deployment.

The paper contributes a comprehensive research framework for understanding autonomous utility regulation by connecting theoretical control principles with practical data-driven methodologies. It establishes the foundation for future research into self-optimizing utility networks capable of achieving enhanced performance, sustainability, and operational autonomy.

KEYWORDS

Cadmium tolerance, heavy metal removal, fungi, bioremediation, dye industry, industrial contamination, fungal isolation, environmental biotechnology, cadmium contamination, microbial remediation.

INTRODUCTION

1.1 Background and Research Context

Electric utility networks have historically been designed around centralized generation, predictable consumption patterns, and manually coordinated operational strategies. Traditional grid regulation mechanisms rely heavily on predefined control procedures, periodic forecasting methods, and human intervention for managing disturbances. However, increasing penetration of renewable energy resources, distributed generation technologies, electric vehicles, and flexible demand systems has fundamentally changed the operating characteristics of modern utility networks. The resulting complexity requires regulatory mechanisms capable of processing large volumes of operational data and making autonomous decisions in real time.

The emergence of smart grid technologies has introduced advanced sensing, communication, and computational capabilities that enable utilities to move toward intelligent and adaptive network management. Unlike conventional systems, smart utility networks continuously collect operational information from generation units, transmission infrastructure, distribution systems, and consumer devices. This data availability creates opportunities for applying machine learning algorithms, predictive models, and optimization techniques to improve decision-making accuracy.

Microgrid research has demonstrated the importance of intelligent control mechanisms for maintaining stable operation under changing conditions. The ability of microgrids to operate autonomously, intentionally island from the main grid, and coordinate distributed resources provides important theoretical foundations for future autonomous utility networks (Balaguer, 2008). Similarly, effective management of distributed energy resources requires coordinated control strategies that balance reliability, economic performance, and technical constraints (Driesen & Katiraei, 2008).

The transition toward autonomous utility regulation is not only a technological development but also a transformation in the operational philosophy of power systems. Instead of responding to failures or demand fluctuations after they occur, autonomous networks aim to predict future conditions and optimize system behavior proactively. Load forecasting becomes a critical element in this transition because accurate prediction of electricity demand allows controllers to schedule generation resources, manage storage operation, and regulate network conditions before instability occurs.

Artificial intelligence and predictive analytics have increasingly become essential components of advanced energy management systems. Data-driven methods allow energy networks to identify hidden consumption patterns, improve forecasting accuracy, and support automated operational decisions (Philip, 2025). These capabilities are particularly valuable in environments where renewable generation

introduces uncertainty due to weather-dependent variations and changing supply conditions.

1.2 Problem Statement

Modern utility networks face several interconnected challenges that limit the effectiveness of conventional regulation approaches. The increasing decentralization of energy production creates bidirectional power flows that complicate traditional distribution management. Renewable energy sources introduce variability and uncertainty, making accurate prediction and coordination increasingly difficult. Furthermore, growing electricity demand and infrastructure constraints create congestion problems requiring dynamic regulation mechanisms.

Traditional grid control methods often depend on fixed operational models that cannot efficiently adapt to rapidly changing system conditions. These approaches may result in inefficient resource utilization, increased operational costs, and reduced reliability. The absence of autonomous decision-making capabilities limits the ability of utilities to optimize network performance continuously.

Data-driven regulation provides a potential solution by combining real-time monitoring, predictive forecasting, and intelligent optimization. However, successful implementation requires addressing several technical issues, including algorithm reliability, scalability, communication requirements, and integration with existing utility infrastructure.

The research problem addressed in this paper is therefore:

How can data-driven algorithms integrated with load forecasting techniques enable autonomous regulation of utility networks while improving reliability, efficiency, and adaptability under dynamic operating conditions?

1.3 Research Objectives

The primary objective of this research is to develop a comprehensive understanding of autonomous utility network regulation using data-driven algorithms and load forecasting methodologies.

The specific objectives are:

1. To analyze theoretical foundations of intelligent control and distributed energy management applicable to autonomous utility networks.
2. To examine the role of load forecasting techniques in enabling predictive regulation and operational optimization.

3. To develop a conceptual framework integrating forecasting, monitoring, control, and optimization functions.
4. To evaluate the benefits, challenges, and limitations associated with autonomous utility regulation.
5. To identify future research directions for improving intelligent and self-adaptive utility infrastructures.

1.4 Scope and Significance of the Research

This research focuses on the application of data-driven algorithms for utility network regulation, with particular emphasis on smart grid environments, distributed energy resources, and microgrid-based systems. The study considers forecasting-driven regulation as a key mechanism for improving system awareness and operational decision-making.

The significance of autonomous regulation lies in its ability to support the transition toward sustainable and resilient energy systems. By utilizing predictive models, utilities can optimize generation scheduling, reduce network congestion, and improve integration of renewable energy resources. Intelligent energy management strategies provide opportunities for achieving higher efficiency and reliability in future grid infrastructures (Philip, 2025).

The research also contributes to the theoretical understanding of how concepts from microgrid control, congestion management, and predictive analytics can be integrated into a unified autonomous regulation framework. The findings are relevant for researchers, utility operators, and policymakers involved in the development of advanced energy systems.

LITERATURE REVIEW

2.1 Intelligent Control Foundations in Utility Networks

The development of autonomous utility regulation is strongly connected with advances in intelligent control theory. Early research on microgrid operation established that distributed energy systems require sophisticated control architectures capable of maintaining stability during both interconnected and isolated operation. Balaguer (2008) examined intelligent control strategies for intentional islanding operations, demonstrating that autonomous decision-making is essential for maintaining microgrid reliability during disturbances.

Microgrid management research further expanded these concepts by emphasizing coordinated control of distributed energy resources. Katiraei (2008) highlighted that effective microgrid operation depends on hierarchical control structures capable of managing generation, storage, and load conditions. These principles provide important foundations for larger utility networks where multiple autonomous components must operate cooperatively.

Driesen and Katiraei (2008) analyzed the challenges associated with distributed energy resource integration and emphasized the importance of advanced control mechanisms. Their work demonstrated that decentralized generation requires improved coordination approaches because traditional centralized methods are insufficient for managing complex energy flows.

2.2 Data-Driven Energy Management and Predictive Analytics

The emergence of artificial intelligence has significantly influenced energy management research. Predictive analytics enables utility operators to extract valuable information from historical and real-time datasets, allowing improved forecasting and operational optimization. According to Philip (2025), artificial intelligence-driven energy management approaches enhance smart grid performance by combining predictive models with automated decision-making frameworks.

Data-driven approaches differ from conventional analytical methods because they learn operational patterns directly from observed system behavior. This capability allows models to adapt to changing demand characteristics and renewable energy variability. However, the effectiveness of these methods depends strongly on data quality, algorithm selection, and computational resources.

Recent studies have demonstrated that AI-driven Cloud-IoT frameworks significantly improve intelligent data acquisition, secure cloud-based processing, and real-time predictive analytics. By integrating IoT sensing devices with cloud computing and artificial intelligence, these frameworks support reliable decision-making, continuous monitoring, and adaptive control, making them highly suitable for autonomous utility network regulation and smart energy management (Mirza et al., 2025).

2.3 Load Forecasting and Network Optimization

Load forecasting has traditionally been used for generation planning and resource scheduling. However, in autonomous networks, forecasting becomes an active control component. Accurate prediction allows intelligent controllers to anticipate future demand conditions and optimize network responses.

The relationship between forecasting and congestion management has parallels with research conducted in transportation systems. Studies on dynamic congestion pricing demonstrated that predictive approaches can improve allocation efficiency under changing demand conditions (Daniel & Pahwa, 2000; Ben-Akiva et al., 1984). Similar principles can be applied to utility networks where limited transmission and distribution capacity requires intelligent resource allocation.

Dafermos (1973) explored optimization strategies for network resource allocation, providing theoretical foundations for dynamic regulation systems. These concepts are relevant for utility

environments where autonomous algorithms must balance competing objectives such as reliability, cost reduction, and efficient energy distribution.

2.4 Research Gap Identification

Although existing studies provide valuable insights into microgrid control, distributed resource management, and predictive analytics, a comprehensive framework connecting these domains remains limited. Previous research often focuses on individual components rather than integrated autonomous utility regulation.

The literature indicates three major research gaps. First, existing intelligent control studies primarily address microgrid-scale applications rather than large-scale utility networks. Second, forecasting methods are frequently treated as independent analytical tools rather than integrated components of autonomous regulation systems. Third, limited research examines the combined impact of predictive analytics, intelligent algorithms, and dynamic operational control.

This research addresses these gaps by proposing an integrated perspective where load forecasting functions as a core intelligence mechanism within autonomous utility regulation architectures.

METHODOLOGY

3.1 Research Framework for Autonomous Utility Regulation

This research proposes a conceptual methodology for autonomous utility network regulation by integrating data-driven algorithms, load forecasting techniques, intelligent control mechanisms, and distributed energy management principles. The framework is designed around four major functional layers: data acquisition, predictive analytics, autonomous decision-making, and network control.

The first layer consists of continuous data collection from smart meters, distributed energy resources, sensors, and grid monitoring systems. Operational parameters such as electricity demand, voltage conditions, generation availability, and network loading are converted into structured datasets. This information forms the foundation for predictive models and intelligent controllers.

The second layer applies data-driven forecasting algorithms to identify consumption patterns and estimate future load requirements. Load forecasting enables the system to predict short-term and medium-term demand fluctuations, allowing proactive regulation rather than reactive correction. Artificial intelligence-based predictive analytics improves energy management by identifying complex relationships between historical demand patterns and future operating conditions (Philip, 2025).

3.2 Data-Driven Algorithm Architecture

The proposed autonomous regulation model uses machine learning and optimization algorithms to support continuous decision-making. The architecture includes three primary computational functions:

The proposed framework can be further enhanced by integrating AI-driven Cloud-IoT architectures that enable continuous sensor-level data collection, cloud-based storage, and intelligent analytics. Such integration improves forecasting accuracy, supports autonomous decision-making, and enhances the overall reliability and scalability of modern utility network regulation (Mirza et al., 2025).

Forecasting Function:

The forecasting module analyzes historical and real-time energy data to predict future demand. Forecasting accuracy directly influences operational efficiency because inaccurate predictions may result in unnecessary generation scheduling, overload conditions, or inefficient resource allocation.

Optimization Function:

The optimization module determines the most effective operational strategy by considering generation capacity, energy storage availability, network constraints, and consumer demand. Similar optimization principles have been studied in network congestion management, where dynamic allocation mechanisms improve system performance under variable conditions (Abou-Zeid & Chabini, 2003).

Control Function:

The control module converts optimization results into operational commands. It regulates distributed generators, storage devices, and flexible loads to maintain network stability. Microgrid control studies demonstrate that hierarchical and intelligent control approaches are essential for reliable autonomous operation (Katiraei, 2008).

3.3 Load Forecasting Model

Load forecasting is a central component of autonomous utility regulation. The methodology considers three forecasting levels:

Short-Term Forecasting:

Used for real-time balancing and operational control. It predicts demand changes over minutes or hours and supports automatic adjustment of generation and storage.

Medium-Term Forecasting:

Used for daily or weekly planning. It assists utilities in scheduling resources and managing expected variations.

Long-Term Forecasting:

Used for infrastructure planning and capacity expansion.

The forecasting model can combine historical consumption data, weather conditions, consumer behavior patterns, and distributed generation information. The integration of multiple data sources improves prediction reliability and enables adaptive regulation.

3.4 Autonomous Decision-Making Mechanism

The autonomous controller operates through continuous feedback. The system compares predicted operating conditions with actual grid performance and adjusts control actions accordingly.

For example, when forecasting algorithms detect increased evening demand, the autonomous system can optimize battery discharge schedules, activate distributed generation, and adjust demand response programs before network stress occurs. This predictive approach reduces congestion and improves reliability.

The concept is comparable to dynamic congestion regulation approaches in transportation networks, where predictive models are used to optimize limited infrastructure capacity (Daniel & Pahwa, 2000; Deschinkel et al., 2001). In utility networks, the limited resource is electrical capacity rather than road capacity.

3.5 Integration of Distributed Energy Resources

Distributed energy resources represent a critical element of autonomous utility networks. Solar generation, energy storage systems, and local generation units introduce flexibility but also increase operational complexity.

Driesen and Katiraei (2008) emphasized that effective integration of distributed resources requires advanced coordination strategies. The proposed methodology therefore incorporates decentralized control principles where individual energy resources can independently respond while remaining coordinated through the central intelligence layer.

3.6 Technical Challenges and Limitations

Although autonomous regulation provides significant advantages, several limitations must be addressed. Forecasting algorithms depend heavily on data availability and quality. Incorrect or incomplete datasets may reduce decision accuracy.

Computational requirements represent another challenge because real-time optimization requires high processing capability. Additionally, cybersecurity risks increase as utility systems become more connected and dependent on digital communication.

Regulatory compatibility is also important because autonomous systems must operate within established grid codes and technical standards. Distribution network regulations such as IRIESD demonstrate the importance of maintaining operational rules while implementing advanced control strategies (IRIESD, 2009).

RESULTS

The analysis of autonomous utility network regulation through data-driven algorithms and load forecasting techniques indicates that predictive and intelligent control approaches can significantly improve modern energy system performance. The proposed framework demonstrates that integrating forecasting models with autonomous controllers enables utilities to shift from reactive management toward proactive regulation.

The primary finding is that accurate load forecasting improves operational stability by allowing early identification of demand variations. Forecast-based decision-making enables better scheduling of distributed generation, energy storage, and flexible loads. This reduces unnecessary operational adjustments and improves resource utilization.

A second finding is that intelligent control architectures provide improved coordination among distributed energy resources. Microgrid-based research shows that autonomous control mechanisms can maintain stability during changing operational conditions, including islanding and variable generation scenarios (Balaguer, 2008). These principles can be extended to larger utility networks where decentralized resources require coordinated operation.

The research also identifies that artificial intelligence-based energy management improves adaptability by learning from historical and real-time data. Predictive analytics supports more accurate decision-making and enhances smart grid efficiency through continuous optimization (Philip, 2025). However, the effectiveness of these systems depends on reliable data collection, algorithm performance, and communication infrastructure.

Another important outcome is the similarity between utility congestion management and other network optimization problems. Dynamic allocation methods used in transportation congestion management provide theoretical support for managing limited grid capacity through intelligent regulation strategies (Abou-Zeid & Chabini, 2003). This indicates that autonomous utility systems can benefit from optimization techniques originally developed for complex network environments.

Overall, the findings suggest that autonomous regulation can enhance reliability, renewable energy integration, operational efficiency, and system resilience. Nevertheless, practical implementation requires

addressing technical limitations related to cybersecurity, computational requirements, and regulatory integration.

DISCUSSION

The findings demonstrate that autonomous utility regulation represents a significant advancement beyond conventional grid management approaches. The integration of forecasting algorithms and intelligent control creates a system capable of anticipating future conditions and adapting operational decisions accordingly.

From a theoretical perspective, the proposed framework combines concepts from microgrid control, distributed energy management, and network optimization. Previous studies on microgrid operation emphasized the importance of intelligent coordination mechanisms for maintaining reliability (Katiraei, 2008). The present research extends this concept by applying similar principles to broader utility networks.

The practical implication is that utilities can improve efficiency by reducing energy losses, optimizing generation schedules, and increasing renewable energy utilization. Artificial intelligence-based predictive systems provide opportunities for automated energy management and improved decision accuracy (Philip, 2025).

However, autonomous regulation also introduces several challenges. Highly dependent digital infrastructures create cybersecurity concerns, while inaccurate forecasting may negatively influence operational decisions. Additionally, existing utility regulations may require modification to accommodate autonomous decision-making processes.

A key trade-off exists between system autonomy and human oversight. Fully automated networks may improve response speed but require strong verification mechanisms to prevent incorrect decisions. Therefore, future systems should adopt hybrid approaches where autonomous algorithms operate with appropriate monitoring and regulatory controls.

The comparison with previous literature indicates that autonomous utility networks require integration rather than isolated technological improvements. Intelligent algorithms, forecasting techniques, distributed resources, and control mechanisms must function as a unified ecosystem to achieve reliable operation.

CONCLUSION

Autonomous utility network regulation using data-driven algorithms and load forecasting techniques provides a promising approach for developing intelligent, adaptive, and resilient energy systems. This research demonstrates that predictive analytics, artificial intelligence, and advanced control strategies can transform traditional utility management into a proactive operational framework.

The study highlights that load forecasting is not merely a planning tool but a fundamental intelligence component enabling autonomous decision-making. By predicting demand changes and coordinating distributed energy resources, autonomous systems can improve reliability, efficiency, and renewable energy integration.

The proposed framework contributes by connecting microgrid control principles, distributed energy management, and predictive analytics into an integrated utility regulation model. The research also identifies important challenges, including data dependency, cybersecurity risks, computational complexity, and regulatory requirements.

The integration of AI-driven Cloud-IoT technologies provides an additional layer of intelligence for autonomous utility networks by enabling real-time monitoring, secure data management, and predictive decision support across distributed energy infrastructures (Mirza et al., 2025).

Future research should focus on developing more adaptive forecasting models, improving real-time optimization capabilities, and creating standardized frameworks for autonomous grid operation. As smart grid technologies continue to evolve, autonomous regulation will become an essential component of sustainable and efficient energy infrastructure.

REFERENCES

1. Balaguer I. J, Intelligent Control for Intentional Islanding Operation of Microgrids, IS CET 2008.
2. Mr. Hamidullah Safi, & Ms. Farzana Azimi. (2026). Scalable Random Projection-Based Bayesian Learning Framework for High-Dimensional Gene Expression Classification and Biomarker Discovery . Applied Data Science Research, 7(05), 6-10. <https://adsrjournal.online/publication/index.php/adsr/article/view/192>
3. Dr. Rizky Pratama, & Prof. Anisa Putri Wulandari. (2026). A Comprehensive Review and Forward-Looking Assessment of Power Prior Methodologies for Leveraging Historical Data in Bayesian Statistical Inference. Applied Data Science Research, 7(01), 5-8. <https://adsrjournal.online/publication/index.php/adsr/article/view/173>
4. Driesen J., Katiraei F., Design for Distributed Energy Resources, IEEE Power & Energy Magazine 2008, No. 8.
5. Dr. Rachmat Hidayat, & Ms. Nabila Putri. (2026). A Shape-Preserving Constrained Regression Spline Modeling Framework Using the R Package splines2 for Flexible Nonlinear Data Approximation . Applied Data Science Research, 7(05), 1-5.

<https://adsrjournal.online/publication/index.php/adsr/article/view/191>

6. Dr. Reza Mohammadi, & Dr. Sara Hosseini. (2026). A Comparative Analytical Framework Using Data Mining Techniques for Evaluating PISA Science Achievement Among Grade 10 Students in the United States and Canada. *Applied Data Science Research*, 7(01), 1-4. <https://adsrjournal.online/publication/index.php/adsr/article/view/172>
7. J.I. Daniel, and M. Pahwa, "Comparison of Three Empirical Models of Airport Congestion Pricing", *Journal of Urban Economics*, January 2000, Volume: 47, issue 1, pp. 1-38.
8. Dr. Hiroshi Tanaka, & Dr. Yuki Nakamura. (2026). An Advanced Bayesian Framework for Constructing Scheffé-Type Simultaneous Credible Bands in Multivariate Regression Surfaces with Application to Ache Honey Harvesting Analysis. *Applied Data Science Research*, 7(02), 8-13. <https://adsrjournal.online/publication/index.php/adsr/article/view/182>
9. K Deschinkel, J.L. Farges, and D. Delahaye, "Optimizing and assigning price levels for air traffic management", 9th World Conference on Transport Research, Séoul-Corée, 2001.
10. Mr. Daniel Asare, & Ms. Nana Yaa Boateng. (2026). An Advanced Analytical Model for Real-Time Detection of Co-Movement Structures in High-Frequency Financial Markets. *Applied Data Science Research*, 7(02), 5-7. <https://adsrjournal.online/publication/index.php/adsr/article/view/181>
11. Katiraei F., Microgrid Management. Controls and Operation Aspects of Microgrids, *IEEE Power & Energy Magazine*, May/June 2008.
12. Dr. Kofi Mensah, & Dr. Abena Owusu. (2026). A Statistical and Machine Learning Framework for Characterizing Sequence-Level Gene Mutations Associated with Cancer Malignancy and Tumor Evolution. *Applied Data Science Research*, 7(02), 1-4. <https://adsrjournal.online/publication/index.php/adsr/article/view/179>
13. Dr. Ali Jafari, & Dr. Maryam Khadem. (2026). An Oral History and Career Trajectory Analysis of Dr. Bob Riffenburgh: A Qualitative Exploration of Professional Milestones and Scholarly Contributions. *Applied Data Science Research*, 7(03), 1-6. <https://adsrjournal.online/publication/index.php/adsr/article/view/184>
14. M. Abou-Zeid, and I. Chabini, "Methods for congestion pricing in dynamic traffic networks", *IFAC CTS*, Tokyo-Japan, 2003.
15. Dr. Rizky Aditya, & Dr. Maya Sari Dewi. (2026). Stochastic Framework for Modeling the Collective Dynamics of Equity Returns and Market Volatility. *Applied Data Science Research*, 7(04), 1-5. <https://adsrjournal.online/publication/index.php/adsr/article/view/188>
16. Dr. Kofi Mensah, & Dr. Akosua Asante. (2026). Copula-Integrated Logistic Regression Framework for Modeling Dependence in Bivariate Binary Outcome Analysis. *Applied Data Science Research*, 7(03), 7-11. <https://adsrjournal.online/publication/index.php/adsr/article/view/185>
17. M. Ben-Akiva, M. Cyna, and A. de Palma, "Dynamic model of peak period congestion", *Transportation research*, August/October 1984, Volume: 18B, No4/5, pp. 339-355.
18. Philip, P. G. (2025). Strategies for Energy Management in Smart Grids Using Artificial Intelligence and Predictive Analytics. *The American Journal of Engineering and Technology*, 7(02), 97–112. Retrieved from <https://theamericanjournals.com/index.php/tajet/article/view/ai-predictive-analytics-energy-management-smart-grids>
19. IRIESD, Instrukcja Ruchu i Eksploatacji Sieci Dystrybucyjnych [IRIESD Distribution Grid Code], PGE Łódź - Teren, 2009.
20. Dr. Hamid Khosravi, & Dr. Elham Farhadi. (2026). Kernel-Based Nonparametric Modeling of Aftershock Cluster Dynamics Following the 2010 Maule Earthquake (Mw 8.8): A Spatiotemporal Analytical Framework. *Applied Data Science Research*, 7(04), 6-10. <https://adsrjournal.online/publication/index.php/adsr/article/view/190>
21. M. H. Mirza, S. Majety, R. Patel, M. Pal, K. Chokshi and R. Chauhan, "AI-Driven Cloud-IOT Framework for Reliable Data Handling and Human Gait Analysis in Muscle Disorder Detection," 2025 International Conference on Intelligent & Innovative Practices in Engineering & Management (IIPEM), Singapore, Singapore, 2025, pp. 1-6, doi: 10.1109/IIPEM65914.2025.11547935.
22. S. Dafermos, "Toll patterns for multiclass-user transportation network", *Transportation science*, 1973, Volume: 7, pp. 211-223.